

## MATH 160 Session #6

Given a quadratic function of the form  $f(x) = a(x - h)^2 + k$ , the graph of  $f$  is a \_\_\_\_\_ that opens \_\_\_\_\_ if  $a > 0$ , opens \_\_\_\_\_ if  $a < 0$  and has its vertex at the point ( \_\_\_\_\_ , \_\_\_\_\_ ).

How can we describe the location and orientation of a quadratic function of the form  $f(x) = ax^2 + bx + c$ ?

Let's do some algebra.

$$\begin{aligned} a(x - h)^2 + k &= a(x^2 - \underline{\hspace{1cm}}x + \underline{\hspace{1cm}}) + k \\ &= ax^2 - \underline{\hspace{1cm}}x + \underline{\hspace{1cm}} + k \\ &= ax^2 + \underline{\hspace{1cm}}x + [\underline{\hspace{1cm}} + k] \end{aligned}$$

In this instance,

$b = \underline{\hspace{1cm}}$  . Solving for  $h$  we obtain  $h = \underline{\hspace{1cm}}$  .

$c = \underline{\hspace{1cm}}$  . Solving for  $k$  we obtain  $k = \underline{\hspace{1cm}}$  .

In conclusion, a quadratic function of the form  $f(x) = ax^2 + bx + c$  has a graph in the shape of a \_\_\_\_\_ that opens \_\_\_\_\_ if  $a > 0$ , opens \_\_\_\_\_ if  $a < 0$ , and has its vertex at the point ( \_\_\_\_\_ , \_\_\_\_\_ ).

For example, here is a sketch of the graph of  $f(x) = -2x^2 + 12x - 3$ .