## Constructing Segments on a Geoboard

How many segments of different lengths can be made by connecting pegs on a square geoboard that is 5 units on each side (a $5 \times 5$ square geoboard)?


Perhaps we should begin by examining simpler cases to see if we can develop a systematic way to generate the different segments. Suppose we start by finding the number of segments of different lengths on a $1 \times 1$ square geoboard, and moving to find the number of segments of different lengths on a $2 \times 2$ square geoboard. We can then continue to consideration of $3 \times 3,4 \times 4$, and $5 \times 5$ square geoboards.


Let's record our results in the table below.

| Size of Geoboard | Number of Segments of Different Lengths |
| :---: | :--- |
| $1 \times 1$ |  |
| $2 \times 2$ |  |
| $3 \times 3$ |  |
| $4 \times 4$ |  |
| $5 \times 5$ |  |

Can we make any relevant conclusions?

