## MATH 100 10-20-2008

In July of 2008 India's population was estimated to be $1,147,995,904$. At that time India's population was estimated to be growing at the rate of $1.578 \%$ per year. Let's approximate India's population at 1.148 billion and assume its annual rate of growth is approximately $1.6 \%$. On that basis we will estimate India's approximate population in billions for the years 2008 to 2018 inclusive.

| Year | Years Since <br> 2008 <br> t | India's Population <br> (billions) <br> $\mathrm{P}(\mathrm{t})$ | $\frac{P(t)}{P(t-1)}$ |
| :---: | :---: | :---: | :---: |
| 2008 | 0 | 1.148 |  |
| 2009 | 1 |  | 1.016 |
| 2010 | 2 |  |  |
| 2011 | 3 |  |  |
| 2012 | 4 |  |  |
| 2013 | 5 |  |  |
| 2014 | 6 |  |  |
| 2015 | 7 |  |  |
| 2016 | 8 |  |  |
| 2017 | 9 |  |  |
| 2018 | 10 |  |  |

$$
\begin{aligned}
\mathrm{P}(1) & =\mathrm{P}(0)+0.016 \mathrm{P}(0) \\
& =(1.016) \mathrm{P}(0) \\
& =(1.016)(1.148) \\
& \approx
\end{aligned}
$$

About when will India's population reach 1.3 billion?
In the situation considered here we refer to $1.6 \%$ as India's growth rate and (1.016) as India's growth factor.

The function defined below can be used to estimate India's population in billions t years after 2008.
$\mathrm{P}(\mathrm{t})=$

Can we estimate when India's population will double?

## Exponential Notation and Working with Exponents

In exercises $1 \& 2$ Calculate each of the following:


$$
2^{-1}=\ldots \quad ; 2^{-2}=\ldots \quad ; 2^{-3}=\ldots \quad ; 2^{-4}=\ldots \ldots ; 2^{-5}+\ldots
$$

2. $10^{4}=$ $\qquad$ $; 10^{3}=$ $\qquad$ ; $10^{2}=$ $\qquad$ ; $10^{1}=$ $\qquad$ $; 10^{0}=$ $\qquad$ ; $10^{-1}=$ $\qquad$ ; $10^{-2}=$ $\qquad$ ; $10^{-3}=$ $\qquad$ $; 10^{-4}=$ $\qquad$
In exercises 3-14 solve for x :
3. $\left(2^{3}\right)^{5}=2^{x}$
4. $\left(2^{3}\right)\left(2^{5}\right)=2^{x}$
5. $\frac{2^{5}}{2^{3}}$
6. $\frac{2^{3}}{2^{5}}$
7. $120,000=1.2\left(10^{x}\right)$
8. $\quad 0.000012=1.2\left(10^{x}\right)$
9. $120,000=1.2\left(10^{x}\right)$
10. $0.0000012=1.2\left(10^{x}\right)$
11. $2^{x}\left(2^{7}\right)=2^{3}$
12. $\left(2^{\mathrm{x}}\right)^{2}=2$.
13. $\left(2^{x}\right)^{3}=2$
14. $8^{\frac{2}{3}}=x$
15. Write in scientific notation: $1,230,000$
16. Write in scientific notation: 0.00000000123
17. Simplify each expression:
a. $x^{3} \cdot x^{5} \cdot x^{-1}$
b. $\frac{x^{7}}{x^{2}} \cdot x^{-3}$
c. $\sqrt{x^{6}}$
