

$$A(0) = \$1000$$

$$A(1) = A(0) + 0.06A(0) = A(0)(1 + 0.06) = A(0)(1.06) = \underline{\hspace{2cm}}$$

$$A(2) = A(1) + 0.06A(1) = A(1)(1 + 0.06) = A(1)(1.06) = A(0)(1.06)^2 = \underline{\hspace{2cm}}$$

$$A(3) = A(2) + 0.06A(2) = A(2)(1 + 0.06) = A(2)(1.06) = A(0)(1.06)^3 = \underline{\hspace{2cm}}$$

⋮

$$A(8) = A(7) + 0.06A(7) = A(7)(1 + 0.06) = A(7)(1.06) = A(0)(1.06)^8 = \underline{\hspace{2cm}}$$

⋮

$$A(t) = A(0)(1.06)^t = 1000(1.06)^t$$

- b. \$1000 is placed in an account that pays interest at the rate of 6% per annum compounded at the end of each month. Let  $t$  = the number of years since the \$1000 was deposited, and let  $A(t)$  = the value of the account in dollars after  $t$  years. Assume that after the initial deposit no further deposits or withdrawals are made.

Since we calculate interest payments at the end of each month we note that the monthly rate corresponding to a per annum rate of 6% is  $6\%/12$  or  $\frac{1}{2}\%$ . Considering the account's status at the end of each month we obtain the following:

$$A(0) = \$1000$$

$$A(1/12) = A(0)(1 + 0.005) = \$1000(1.005) = \underline{\hspace{2cm}}$$

$$A(2/12) = A(0)(1.005)^2 = \$1000(1.005)^2 = \underline{\hspace{2cm}}$$

⋮

$$A(1) = A(0)(1.005)^{12} = \$1000(1.005)^{12} = \underline{\hspace{2cm}}$$

⋮

$$A(t) = A(0)(1.005)^{12t} = \$1000(1.005)^{12t}$$

Under this compounding scheme about how long will it take for the value of the account to double?

- c. \$1000 is placed in an account that pays interest at the rate of 6% per annum compounded  $n$  times per year. Let  $t$  = the number of years since the \$1000 was deposited, and let  $A(t)$  = the value of the account in dollars after  $t$  years. Assume that after the initial deposit no further deposits or withdrawals are made.

Since there are  $n$  compounding periods per year the interest rate per period is  $6\%/n$ , or  $0.06/n$ , and in  $t$  years there will be  $nt$  interest calculations. So, in this case we have

$$A(0) = \$1000$$

$$A(t) = A(0)(1 + 0.6/n)^{nt}$$

Suppose we have daily compounding. Calculate the value of

$$A(1) = \$1000(1 + 0.06/360)^{360(1)}.$$

- d. In general, if  $A(0)$  is placed in an account that pays interest at the rate of  $r$  per annum compounded  $n$  times per year, then  $A(t)$  = the value of the account in dollars after  $t$  years is given by  $A(t) = A(0)(1 + r/n)^{nt}$ . Suppose  $A(0) = 1000$ ,  $r = .04$ , and  $n = 360$ . Find  $A(1)$  and  $A(8)$ .