MATH 210 Discrete Mathematics - Session 6

Which arguments appear vaild?

If the sum of the digits of this number is divisible by	y 9,	then t	his	numbei	r is
divisible by 3.					

The sum of the digits of this number is divisible by 9.

This number is divisible by 3. *:*.

$$p \Rightarrow q$$

$$q$$

:.

If the sum of the digits of this number is divisible by 9, then this number is divisible by 3.

This number is not divisible by 3.

The sum of the digits of this number is not divisible by 9. ∴.

$$p \Rightarrow q$$

$$\sim q$$

$$\sim p$$

:.

:.

(4)

(5)

If the sum of the digits of this number is divisible by 9, then this number is divisible by 3.

This number is divisible by 3.

The sum of the digits of this number is divisible by 9. *:*.

$$p \Rightarrow q$$

$$q$$

$$p$$

Give a reason for each step.

$$(1) ab = 0 and b \neq 0$$

a = 0 or b = 0

premise

$$(2) \qquad ab = 0$$

(3) If
$$ab = 0$$
 then $a = 0$ or $b = 0$.

$$\mathbf{(5)} \qquad \mathbf{b} \neq \mathbf{0}$$

$$(6) \qquad \mathbf{a} = \mathbf{0}$$

(7) : If
$$ab = 0$$
 and $b \neq 0$ then $a = 0$.