

## 8) Understanding the Problem

Construct a table using the data and examine the pattern to determine which method works best. Then make a functional equation to determine the number of cubes in the 100<sup>th</sup> figure.

### Devising A Plan

I am going to make a table, figure out the pattern, and then make an equation based on the pattern. Then I will be able to plug 100 in for "n" to get the number of cubes in the 100<sup>th</sup> figure.

### Carrying out the Plan

1	2	3	4	5
1	4	7	10	13

3      3      3      3

Key

$Q_1$  = The first term is 1

$Q_n$  = The n<sup>th</sup> term

$Q_{n-1}$  = The term before

- (A) The method of finite differences can be used because there is a common difference and the data is expressed with a linear line on a graph. With this method we can infer that:

$$Q_1 = 1$$

$$Q_n = Q_{n-1} + 3 \leftarrow \text{arithmetic sequence}$$

(C)  $Q_n = 3n - 2 \leftarrow \text{Functional equation}$

(B)  $Q_n = 3(100) - 2 \rightarrow$  So, there are 298 cubes in the 100<sup>th</sup> figure.

### Looking Back

With the functional equation we can figure out that the 1,000<sup>th</sup> figure has 2998 cubes in it.