

Basis & Dimension of a Subspace

A *basis* for a subspace H of \mathbb{R}^n is a linearly independent set in H that spans H .

If $A = \begin{bmatrix} 1 & -1 & 0 & 0 \\ 0 & 1 & -2 & 2 \\ 0 & 2 & -4 & 4 \end{bmatrix}$ find a basis for $Col A$ and also for $Nul A$.

Claim: The pivot columns of a matrix A form a basis for $Col A$.

The *dimension* of a nonzero subspace H , denoted by $\dim H$, is the number of vectors in any basis for H . The dimension of the zero subspace $\{\mathbf{0}\}$ is defined to be zero.

Find $\dim Col A$ and also $\dim Nul A$.

The *rank* of a matrix A , denoted by $\text{rank } A$, is $\dim Col A$.

Find $\text{rank } A$.