1. Find the following integral. Keep your answer in exact form.

$$\int_0^2 (2x-3)(4x^2+1) \, dx$$

Solution:

$$\int_{0}^{2} (2x-3)(4x^{2}+1) \, dx = \int_{0}^{2} 8x^{3} - 12x^{2} + 2x - 3 \, dx = \left(2x^{4} - 4x^{3} + x^{2} - 3x\right)\Big|_{0}^{2} = -2$$

2. Find the following integral.

$$\int \frac{\cos(x)}{1+\sin(x)} \, dx$$

Solution: Let $u = 1 + \sin(x)$, then $du = \cos(x) dx$

$$\int \frac{\cos(x)}{1+\sin(x)} \, dx = \int \frac{du}{u} = \ln|u| + C = \ln|1+\sin(x)| + C$$

3. Find the following integral.

$$\int \frac{1+x}{1+x^2} \, dx$$

Solution:

$$\int \frac{1+x}{1+x^2} dx = \int \frac{1}{1+x^2} dx + \int \frac{x}{1+x^2} dx$$

= $\tan^{-1}(x) + \frac{1}{2} \int \frac{1}{u} du$ $u = 1+x^2$
= $\tan^{-1}(x) + \frac{1}{2} \ln|u| + C$
= $\tan^{-1}(x) + \frac{1}{2} \ln(1+x^2) + C$

4. Find the following integral.

$$\int x e^{2x} dx$$

Solution: Let u = x and $dv = e^{2x} dx$, then du = dx and $v = \frac{1}{2}e^{2x}$

$$\int xe^{2x} dx = \frac{1}{2}xe^{2x} - \int \frac{1}{2}e^{2x} dx = \frac{1}{2}xe^{2x} - \frac{1}{4}e^{2x} + C$$

5. Find the volume of the solid obtained by rotating the region bounded by $y = x^3$, y = 0, and x = 1 about the x-axis. Keep your answer in exact form.



Solution: Using the disk/washer method, we would have

$$V = \int_0^1 \pi (x^3)^2 \, dx = \pi \int_0^1 x^6 \, dx = \pi \frac{x^7}{7} \Big|_0^1 = \frac{\pi}{7}$$