

1. (10 pt.)

a) $f(n) = O(g(n))$

- $O(g(n)) = \{f(n) \mid \text{there exist positive constant } c \text{ and } n_0 \text{ such that } 0 \leq f(n) \leq cg(n) \text{ for all } n \geq n_0\}$. $g(n)$ is upper bound of $f(n)$

b) $f(n) = \Theta(g(n))$

- $\Theta(g(n)) = \{f(n) \mid \text{there exist positive constant } c_1, c_2 \text{ and } n_0 \text{ such that } 0 \leq c_1g(n) \leq f(n) \leq c_2g(n) \text{ for all } n \geq n_0\}$. $g(n)$ is tight bound of $f(n)$

c) $f(n) = \Omega(g(n))$

- $\Omega(g(n)) = \{f(n) \mid \text{there exist positive constant } c \text{ and } n_0 \text{ such that } 0 \leq cg(n) \leq f(n) \text{ for all } n \geq n_0\}$. $g(n)$ is lower bound of $f(n)$

2. (5 pt.)

Sol) By asymptotic notation, we need show that there exist constant C_1, C_2 and n_0 such that

$$C_1n^2 \leq n^2 + 2n \leq C_2n^2 \text{ for all } n_0 \geq 0$$

$$C_1n^2 \leq n^2 + 2n, \quad \text{where } C_1 = 1 \text{ with } n_0 = 1$$

$$n^2 + 2n \leq C_2n^2, \text{ where } C_2 = 2 \text{ with } n_0 = 2$$

$$C_1n^2 \leq n^2 + 2n \leq C_2n^2 \text{ with } C_1 = 1, C_2 = 2, n_0 = 2 \text{ true}$$

3. (5 pt.)

Sol) By asymptotic notation, there exist constant C , and n_0 such that

$$\frac{1}{2}n^2 - 3n \leq Cn^2 \text{ with } C = 1 \text{ and } n_0 = 1, \text{ it is true}$$

4. (15 pt.) What will each of the following programs display on the screen?

a) Different

```
#include <iostream>
using namespace std;
int main()
{
    char yourName[20] = "Mary";
    char myName[20]="Mary";
    if (yourName == myName)
        cout << "Same"<<endl;
    else
        cout <<"Different"<<endl;
    return 0;
}
```

b)

```
#include <iostream>
using namespace std;
int main()
{
    int num1 = 5;
    int num2 = 5;
    cout <<--num1 <<++num2<<endl;
    cout <<num1-- << num2++<<endl;
    return 0;
}
4 6
4 6
```

c)

```
#include <iostream>
using namespace std;
int main ()
{
    int cnt;
    for (cnt = 1; cnt <= 10; cnt++){
        if (!(cnt % 4 == 0))
            cout << cnt << " " <<endl;
    }
    return 0;
}
1 2 3 5 6 7 9 10
```

d)

```
#include <iostream>
using namespace std;
int main()
{
    char *ptr ={"good for you?"};

    cout << ptr+1 <<endl;
    cout << *(ptr+2) <<endl;
    return 0;
}
ood for you
o
```

e)

```
#include <iostream>
using namespace std;
int main ()
{
    for (int i = 1; i <= 10; i++){
        if (i % 4 ==0)
            break;
        cout << i << ' ';
    }
    return 0;
}
1 2 3
```

f)

```
#include <iostream>
using namespace std;

int main()
{
    char *ptr[2] ={"123456", "789" };
    cout << ptr[0]+2 <<endl;
    return 0;
}

3456
```

g)

```
#include <iostream>
using namespace std;
int main()
{
    int a[5] ={1,2,3,4,5};
    int *ptr;
    ptr = a+1;
    ptr=ptr+2;
    cout << *ptr<<endl;
    return 0;
}
4
```

h)

```
#include <iostream>
using namespace std;

int main()
{
    char *ptr[2] ={"ABCDEF", "GHIJK" };
    cout << *(ptr+1) <<endl;
    return 0;
}
GHIJK
```

5. (15 pt.)

```

bool Palindrome (char A[], int Size)
{
    int front =0;
    int back =Size -1;
    bool rval;
    while ((A[front]==A[back]) && (front <= back))
    {
        front++;
        back --;
    }
    if (front > back)
        rval = true;
    else
        rval = false;
    return rval;
}

```

6. (10 pt)

Insertion Sort	Selection Sort	Bubble Sort
8, 6, 2, 3, 4, 5, 7	8, 6, 2, 3, 4, 5, 7	8, 6, 2, 3, 4, 5, 7
6, 8, 2, 3, 4, 5, 7	2, 6, 8, 3, 4, 5, 7	6, 2, 3, 4, 5, 7, 8
2, 6, 8, 3, 4, 5, 7	2, 3, 8, 6, 4, 5, 7	2, 3, 4, 5, 6, 7, 8
2, 3, 6, 8, 4, 5, 7	2, 3, 4, 6, 8, 5, 7	2, 3, 4, 5, 6, 7, 8
2, 3, 4, 6, 8, 5, 7	2, 3, 4, 5, 8, 6, 7	2, 3, 4, 5, 6, 7, 8
2, 3, 4, 5, 6, 8, 7	2, 3, 4, 5, 6, 8, 7	2, 3, 4, 5, 6, 7, 8
2, 3, 4, 5, 6, 7, 8	2, 3, 4, 5, 6, 7, 8	2, 3, 4, 5, 6, 7, 8

7. (10 pt.)

```
void selectionSort (int A[], int size)
{
    int min,tmp;
    for (int j = 0; j < size -1; j++)
    {
        min = j;
        for (int k= j+1; k <= size -1; k++)
        {
            if (A [k] < A[min])
                min = k;
        }
        if (min != j)
        {
            tmp = A[j];
            A[j] = A[min];
            A[min] = tmp;
        }
    }
}
```

8. (5 pt.)

(Answer)

- Text section – executable code
- Data section – Global variable and Static variables
- Heap – space for dynamic memory allocation
- Stack section – store local variables when a function all

9. (15 pt)

```
Node *DeleteNode (Node *List, int ID)
{
    Node *Tmp = List;

    // Case 1: List is empty
    if (List == NULL)
        cout << "Empty List" <<endl;
    //Case 2: Delete the first node
    else if (Tmp->IDNumber == ID)
    {
        List = List->Next;
        delete Tmp;
    }
    else
    {
        while (Tmp->Next !=NULL && Tmp->Next->ID != ID)
            Tmp = Tmp->Next;
        // Case 3: No Such a node
        if (Tmp ->Next == NULL)
            cout <<"There is no student with ID number: "<<ID <<endl;
        // Case 4: Delete a node from a list (not first node)
        else if (Tmp ->Next->IDNumber == ID)
        {
            Node *T = Tmp->Next;
            Tmp->Next = Tmp->Next->Next;
            delete T;
        }
    }
    return List;
}
```

10. (10 pt.)

<pre> #include <iostream> using namespace std; void funA(int, int); void funB(int); class test { public: int a; test(int); ~test(); }; // constructor test::test(int x) { a = x; cout << a <<" is created" <<endl; } // destructor test::~~test() { cout << a << " is destroyed" <<endl; } </pre>	<pre> // main int main() { test a(10); funA(20, 30); funB(40); return 0; } //funA void funA(int x, int y) { test a(x); test *ptr = new test (x+1); funB (y); delete (ptr); } // funB void funB(int x) { test a(x); test *ptr = new test(x+1); } </pre>
--	--

10 is created
 20 is created
 21 is created
 30 is created
 31 is created
 30 is destroyed
 21 is destroyed
 40 is created
 41 is created
 40 is destroyed
 10 is destroyed